Electric Fields

Self Evaluation Exercise 13.2 (p.11)

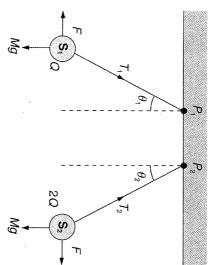
due to another point charge Q is: The Coulomb's force experienced by a point charge q

$$F = \frac{Qq}{4\pi\varepsilon_0 x^2}$$
$$F \propto \frac{1}{x^2}$$

When - $\frac{1}{x^2}$ increases, the force F increases.

2.

The force diagram of the system is:



experienced by each sphere is the same. According to Newton's Law, the Coulomb's force

To balance the forces,
$$T_{1} = 266 A - M_{2}$$

$$T_1 \cos \theta_1 = Mg$$

 $T_2 \cos \theta_2 = Mg$
 $T_1 \sin \theta_1 = F$

$$T_1 \sin \theta_1 = F$$
$$T_2 \sin \theta_2 = F$$

$$T_2\sin\theta_2 = F$$

$$T_2 \sin \theta_2 = F$$
 $T_2 \sin \theta_2 = F$

$$\frac{T_1 \sin \theta_1}{T_1 \cos \theta_1} = \frac{T_2 \sin \theta_2}{T_2 \cos \theta_2} = \frac{F}{Mg}$$

$$\tan \theta = \tan \theta$$

$$\tan \theta_1 = \tan \theta_2$$

$$\theta_1 = \theta_2$$

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Similar to Question 2.

the same. are, the Coulomb's force experienced by each sphere is No matter how much the quantity of charge on X and Y

$$T_X \sin \alpha = T_Y \sin \beta = F$$
 $T = \sin \beta$

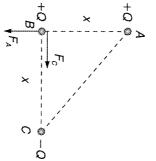
$$\frac{T_X}{T_Y} = \frac{\sin \beta}{\sin \alpha}$$

And
$$T_X \cos \alpha = M_X g$$

 $T_Y \cos \beta = M_Y g$
 $\therefore \frac{M_X}{M_Y} = \frac{T_X}{T_Y} \cdot \frac{\cos \alpha}{\cos \beta}$
 $= \frac{\sin \beta}{\sin \alpha} \cdot \frac{\cos \alpha}{\cos \beta}$
 $= \frac{\tan \beta}{\tan \alpha}$
 $\therefore \alpha > \beta \therefore \tan \alpha > \tan \beta \text{ (Both } \alpha, \beta < 90^\circ)$
 $\therefore m_X < m_Y$

4. \bigcirc

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downwards (repulsion). direction. F_C points to the right (attraction) and F_A points to the charge at A and C are the same. But they differ in The magnitudes of the Coulomb's force acted on B due

(a) The magnitude of resultant force is: $(F_A)^2 + (F_C)^2 = (F_R)^2$

$$\sqrt{2} \left(\frac{Q^2}{4\pi\varepsilon_0 x^2} \right) = F_R$$

$$= \frac{\sqrt{2}Q^2}{4\pi\varepsilon_0 x^2}$$

$$= \frac{\sqrt{2}(2 \times 10^{-7})^2}{4\pi(8.85 \times 10^{-12})(0.1)^2}$$

 $\Pi_{\mathbf{A}}$ 45° π_{o1}

 $= 0.0509 \,\mathrm{N}$

$$tan\theta = \frac{F_C}{F_A} = 1 \quad \therefore \quad \theta = 45^{\circ}$$

The electrostatic force between 2 protons is:

$$_{\rm e} = \frac{Q_1 Q_2}{4\pi \varepsilon_0 x^2} = \frac{(Q_{\rm p})^2}{4\pi \varepsilon_0 x^2} (Q_{\rm p} - {\rm charge \ of \ a \ proton})$$
 1.

The gravitational force between them is:

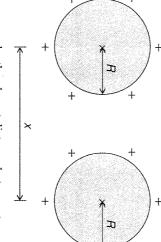
2.

$$F_{\rm g} = \frac{Gm_1m_2}{x^2} = \frac{G(m_{\rm p})^2}{x^2} \ (m_{\rm p} - \text{mass of a proton})$$
The ratio is:

$$\frac{F_{\rm e}}{F_{\rm g}} = \frac{(Q_{\rm p})^2}{G(m_{\rm p})^2 4\pi\varepsilon_0}$$

$$=\frac{(1.6\times10^{-19})^2}{6.67\times10^{-11}\times(1.67\times10^{-27})^2\times4\pi(8.85\times10^{-12})}$$
$$=1.23\times10^{36}$$

.7 x apart. The charges are evenly distributed on the spheres' surfaces. Because the system is not two point charges at a distance



For example, the closest distance between two spheres is x - 2R and the farest distance is x + 2R. After squaring of 1. To study the electric field at point P, a positive R and R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance is R + 2R. After squaring of R are the farest distance in R and R are the farest spheres surface does not equal to F =distance, the force due to the charges at points on the $4\pi\varepsilon_0x^2$.

(a) Charging by friction refers to the seeds loosing surrounding, and so acquiring a positive charge. electrons due to friction between the seeds and their

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3 Electric force = weight

i.e.
$$\frac{ee}{4\pi\varepsilon_0 x^2} = mg$$

$$\Rightarrow x^2 = \frac{ee}{4\pi\varepsilon_0 mg}$$

$$= \frac{(1.60 \times 10^{-19})(1.60 \times 10^{-19})}{4\pi (8.85 \times 10^{-12})(9.0 \times 10^{-14})(9.81)}$$

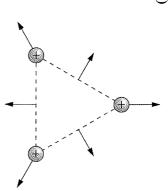
$$= 2.607 \times 10^{-16}$$

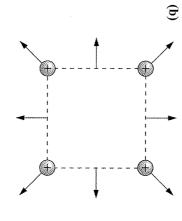
$$\therefore x = \sqrt{2.607 \times 10^{-16}}$$

$$= 1.614 \times 10^{-8} \text{ m} = 16 \text{ nm}$$

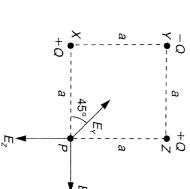
Self Evaluation Exercise 13.3 (p.14)

direction to the electric field. The electric force on a negative charge is opposite in





electric field. And the resultant field can be calculated by charge is placed at point P to decide the direction of To study the electric field at point P, a positive test vector addition.

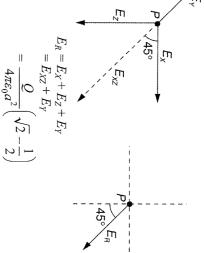


Since the distance between *P* and *X* is the same as that of P and Z, the magnitude of electric field is the same:

$$\frac{Q}{4\pi\varepsilon_0 a^2}$$

And the electric field due to charge at point Y is:
$$\frac{Q}{4\pi\varepsilon_0(\sqrt{2}a)^2} = \frac{Q}{4\pi\varepsilon_0a^2(2)}$$

The resultant field (E_R) is:



(a)

0.15 m X Ш

charge is the same as that of negative charge. The magnitude of electric field due to positive The magnitude of total electric field is:

$$\left(\frac{q}{4\pi\varepsilon_0 x^2}\right) = \frac{2 \times 10^{-7}}{2\pi (8.85 \times 10^{-12}) \times (0.15 \div 2)^2}$$
$$= 6.39 \times 10^5 \text{ N C}^{-1}$$

The direction of electric field is along the negative charge.

(b) The magnitude of force is:

$$F = Eq$$
= (6.39 × 10⁵)(1.6 × 10⁻¹⁹)
= 1.02 × 10⁻¹³ N

direction of electric field. It is towards the positive The direction of force is opposite to the The electron is negatively charged.

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charges. Point of zero field will be further away from the point charge of smaller magnitude (Q). Electric field will not be zero between two opposite point charge of greater magnitude (-2Q) than from the

Self Evaluation Exercise 13.5 (p.28)

For a point charge:

$$E = \frac{Q}{4\pi\varepsilon_0 r^2} \text{ and } V = \frac{Q}{4\pi\varepsilon_0 r}$$

unit positive charge from infinity to that point. Electric potential at a point is the work done to move a

$$V = \frac{W}{q}$$

$$= \frac{15}{3} = 5 \text{ J C}^{-1} = 5 \text{ V}$$

Electric potential is a scalar quantity.

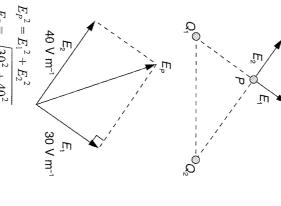
simply scalar addition: The total electric potential due to Q_1 and Q_2 is

$$V_P = V_1 + V_2$$

= 60 + 120

Electric field is a vector quantity. = 180 V

by vector addition. The total electric field due to Q_1 and Q_2 is calculated

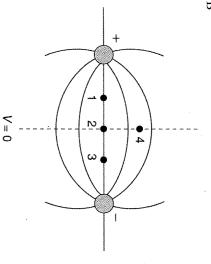


 $E_P = \sqrt{30^2 + 40^2}$ $= 50 \text{ V m}^{-1}$

D ٠: E =dVdx

electric potential with distance) is negative. In other direction of electric field, the slope (the rate of change of electric potential decreases. words, along the direction of electric field line, the The negative sign of the equation means that along the

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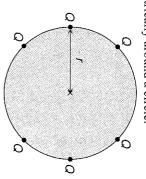


addition of electric potential due to positive charge and The resultant electric potential of each point is the also due to negative charge at that point.

zero.

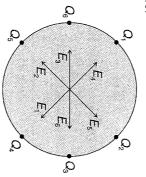
- electric potential is zero. At the mid-point between the two charges, the
- $V_2 = V_4 = 0$
- On the right side from the central axis, the electric potential is negative. On the left side, electric potential is positive.
- and 3. The greatest potential difference is between points 1
- 6. A
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- 9. B
- 10. (a)
- Ξ Ξ

- 11. Yes. These are two examples. (1) The system of six identical charges Q placed
- symmetrically around a circle.



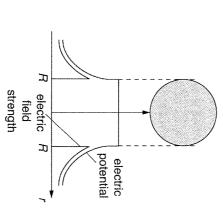
not zero. However, the electric field at the centre is At the centre, the electric potential is $\frac{6Q}{1-Q}$. It is $4\pi\varepsilon_0 r$

zero. By symmetry, the resultant electric field is The charges are equally apart from the centre.



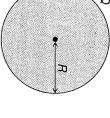
(2) Inside a charged conducting sphere, E_1 cancels E_4 , E_2 cancels E_5 and E_3 cancels E_6 . Magnitude: $E_1 = E_2 = E_3 = E_4 = E_5 = E_6$

$$V = \frac{Q}{4\pi\varepsilon_0} \cdot \frac{1}{R} \text{ and } E = 0$$



sphere. By symmetry, the electric field strength is Electric potential is constant inside the conducting

> 12. **a**



The definition of electric potential is:

$$V = \frac{\frac{\varkappa}{4\pi\varepsilon_0 x}}{4\pi\varepsilon_0 x}$$

$$500 = \frac{3\times10^{-11}}{4\pi(8.85\times10^{-12})R}$$

(b) The charge of the new drop is double that of the drop is also double that of the original drop. The volume of a sphere is: original one. And the volume of the larger spherical

 $R = 5.39 \times 10^{-4} \text{ m}$

$$Vol = \frac{4}{3} \pi R^3 \propto R^3$$

And the electric potential is:

$$r = \frac{Q}{4\pi\varepsilon_0 R} \Rightarrow V \propto \frac{Q}{R} \Rightarrow R \propto \frac{Q}{V}$$

$$\left(\frac{\text{Vol}_{\text{large}}}{\text{Vol}_{\text{original}}}\right)^{\frac{1}{3}} = \frac{R_{\text{large}}}{R_{\text{original}}} = \frac{V_{\text{original}}}{V_{\text{large}}} \cdot \frac{Q_{\text{large}}}{Q_{\text{original}}}$$

$$\frac{V_{\text{original}}}{V_{\text{large}}} \cdot \frac{Q_{\text{large}}}{Q_{\text{original}}} = \left(\frac{\text{Vol}_{\text{large}}}{\text{Vol}_{\text{original}}}\right)^{\frac{1}{3}}$$

$$\frac{V_{\text{original}}}{V_{\text{large}}} \cdot (2) = 2^{\frac{1}{3}}$$

$$V_{\text{large}} = \frac{2(50)}{V_{\text{large}}} \cdot (2) = 2^{\frac{1}{3}}$$

$$V_{\text{large}} = \frac{2(500)}{\frac{1}{3}}$$
$$= 794 \text{ V}$$

- 13. (a) (i) Sketch as solid arrows radiating out from sphere, labelled E.
- (ii) Sketch as concentric circles in dashed lines with increasing spacing, labelled V.

(b) (i) Calculate Vx in 3^{rd} column:

39	32	25	19	x/cm
0.73×10^5	0.89×10^{5}	1.14×10^{5}	1.50×10^{5}	V/A
28.5×10^{5}	28.5×10^{5}	28.5×10^{5}	28.5×10^5	V_X/V cm

 $V_X = 28.5 \times 10^5 = \text{constant}$

$$\Rightarrow V \otimes \frac{1}{\sqrt{1}}$$

(ii) $V_{\text{surface}} r = \text{constant} (28.5 \times 10^5)$

.. Radius of sphere,

$$r = (28.5 \times 10^5) \div (1.9 \times 10^5) = 15 \text{ cm}$$

$$V = \frac{Q}{4\pi\varepsilon_0 r}$$

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$$Q = 4V\pi\varepsilon_0 r$$
= $4(1.9 \times 10^5)\pi (8.85 \times 10^{-12})(15 \times 10^{-2})$
= $3.17 \times 10^{-6} C$

Self Evaluation Exercise 13.7 (p.35)

The electric potential due to 1 charge Q at the centre is:

$$\frac{Q}{4\pi\varepsilon_0 r}$$

 $\frac{18}{4\pi\varepsilon_0 r}$. electric potential at the centre due to the 6 charges QElectric potential is a scalar quantity. The total <u>0</u>

And the work done to remove a point charge
$$q$$
 is:
$$W = Vq = \frac{6Qq}{4\pi\varepsilon_0 r}$$

4

The electric force between two protons is:

$$F = \frac{Q_1 Q_2}{4\pi\varepsilon_0 x^2} = \frac{(1.6 \times 10^{-19})^2}{4\pi (8.85 \times 10^{-12})(1.5 \times 10^{-15})^2}$$
$$= 102.3 \text{ N}$$

The electric potential due to a proton at a distance x is:

And the work done against the force to bring the other proton at distance
$$1.5 \times 10^{-15}$$
 m is:

 $4\pi\varepsilon_0 x$

W = Vq = -

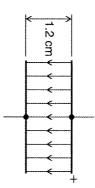
$$= \frac{Q_1}{4\pi\varepsilon_0 x} \cdot Q_2$$

$$= \frac{(1.6 \times 10^{-19})^2}{4\pi (8.85 \times 10^{-12})(1.5 \times 10^{-15})}$$

$$= 1.53 \times 10^{-13} \text{ J}$$

Self Evaluation Exercise 13.8 (p.38)

1. (a) (i) Mark the upper plate as more positive.



(ii)
$$E = \frac{V}{d}$$

p.d. between plates,

(b) Let $a_e =$ acceleration of an electron Force = $mass \times acceleration$ $V = Ed = (3.0 \times 10^4)(0.012) = 360 \text{ V}$

ı.e.

$$eE = m_e a_e$$

$$a_e = \frac{eE}{m_e} = \frac{(1.60 \times 10^{-19})(3.0 \times 10^4)}{9.11 \times 10^{-31}}$$

$$= 5.3 \times 10^{15} \,\mathrm{m \, s^{-2}}$$

Self Evaluation Exercise 13.9 (p.46)

$$P_{\odot} \xrightarrow{F} F$$
 X-direction $q \xrightarrow{F} E$

positive charge. By definition, electric field is the force acting on a unit

$$E = \frac{F}{q} \quad \therefore F = Eq$$

bring a unit positive charge from infinity to that point. Electric potential at a point is the energy required to

$$V = \frac{U}{q} \quad \therefore \ U = Vq$$

And suppose the displacement is small, then displacement, there is a negative sign in the equation. force acting on it times the displacement. Because the direction of the force is opposite to that of the The work done of moving a charge from infinity is the

$$dU = -Fdx \quad \therefore F = -\frac{dU}{dx}$$

And
$$F = -\frac{dU}{dx}$$

$$qE = -\frac{dU}{dx}$$

$$E = -\frac{dU}{dx} = -\frac{dV}{dx}$$

2

not be equal to zero. An example is the case inside a When the electric potential is zero, the electric field may charged conducting sphere.

Choice A (incorrect)

units are Joule per Coulomb and Volt. Joule is not the unit of electric potential. The correct

Choice B (incorrect)

Choice C (incorrect) the rate of change of electric potential with distance. The correct statement is that the electric field is given by

be the work done to move a unit positive charge from infinity to the point. By the definition of electric potential at a point, it should

4. A
$$E = -\frac{dV}{dx} \Rightarrow \int_{p}^{Q} E dx = -\int_{p}^{Q} dV = \int_{Q}^{p} dV = V_{p} - V_{Q}$$
The shaded area

between P and Q

It represents the potential difference between P and \mathcal{O}

6 where $-\frac{dV}{2}$ E =dVdx

 $\frac{dx}{dx}$ is the slope of curve.

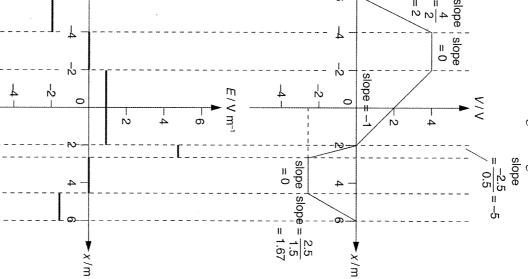
conductor is not the same everywhere, then $\frac{dV}{dt}$

 $-\neq 0$.

If the electric potential on the surface of a charged

dx

the electric field strength is negative. The negative sign means that when the slope is positive,



the same. The electric potential at any point inside a conductor is

And
$$E = -\frac{dV}{dx}$$

$$\therefore$$
 V is constant, $\frac{dV}{dx} = 0$

$$E = 0$$

case is not applicable to static charge (electrostatic). a force to move charge inside the conductor. Then, the must be zero inside a conductor. Otherwise, there will From another point of view, the electric field strength be

not static and it is not the case for electrostatic.

charges to move from a point to another. The charges are And there is resultant electric field that would drive the

(a) Coulomb force is the force between charged particles:

$$\vec{r}_{\rm C} = \frac{1}{4\pi\varepsilon_0} \cdot \frac{Q_1 Q_2}{r^2} \propto \frac{1}{r^2}$$

Gravitational force is the force between masses:

$$=\frac{GM_1M_2}{r^2}\propto\frac{1}{r^2}$$

 $F_{\rm G} = \frac{GM_1M_2}{r^2} \propto \frac{1}{r^2}$

$$r^2$$
 r^2
y, both forces are directly propo

to $\frac{1}{r^2}$ (obeys inverse square law). That means if the For similarity, both forces are directly proportional

masses has the tendency to move towards each distance between 2 charges (masses) doubles, the between masses must be attractive. This means repulsive. The force between like charges (+, +), For difference, Coulomb force can be attractive or force between them is decreased by 4 times. (+, −) is attractive. However, gravitational force (-, -) is repulsive. The force between unlike charges

ਭ In Hydrogen atom, there is one proton and one electron. The magnitude of charge of a proton is equal to that of an electron.

The magnitude of the Coulomb force is:

gnitude of the Coulomb force is:
$$F_{\rm C} = \frac{1}{1} \cdot \frac{Q_{\rm p}Q_{\rm e}}{Q_{\rm e}}$$

$$= \frac{(1.6 \times 10^{-19})^2}{4\pi (8.85 \times 10^{-12})(5.3 \times 10^{-11})^2}$$
$$= 8.19 \times 10^{-8} \,\mathrm{N}$$

The magnitude of the gravitational force is: $GM_{
m p}M_{
m e}$

=
$$\frac{(6.67 \times 10^{-11})(1.673 \times 10^{-27})(9.11 \times 10^{-31})}{(5.3 \times 10^{-11})^2}$$

= 3.62×10^{-47} N

The ratio between $F_{\rm C}$ and $F_{\rm G}$ is:

$$\frac{F_{\rm C}}{F_{\rm G}} = \frac{8.19 \times 10^{-8}}{3.62 \times 10^{-47}} = 2.26 \times 10^{39} \sim 10^{39}$$

$$F_{\rm E} = Eq$$

The weight of electron is mg .

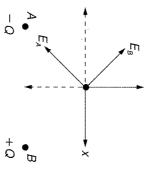
e weight of electron is
$$mg$$
.
 $F_{\rm E}=1.6~mg$
 $Eq=1.6~mg$

$$E = \frac{1.6 \times (9.11 \times 10^{-31}) \times 9.8}{1.6 \times 10^{-19}}$$
$$= 8.9 \times 10^{-11} \text{ V m}^{-1}$$

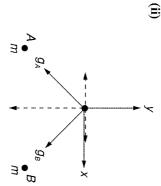
- .2 a Electric field at a point is the force acting on a unit of positive charge at that point.
- unit of mass at that point. Gravitational field at a point is the force acting on a Unit for electric field is N C⁻¹.
- charge from infinity to that point. work done (energy) required to move a unit positive Electric potential at a point in an electric field is the Unit for gravitational field is N kg⁻¹
- Unit for electric potential is J C⁻¹

bring a unit mass from infinity to that point field is the work done by the gravitational force to Gravitation potential at a point in a gravitational

(b) (i) Unit for gravitational potential is J kg⁻¹.



x-direction. the fields into x and y components, the yThe resultant electric field points to negative components of two field cancel each other. A and B are equidistant from C. After breaking



the fields due to two masses point to the components, the resultant field points to masses. After breaking the field into Since gravitational force is always attractive, negative y-direction.

(iii) The electric potentials due to the charges at A and B are:

$$V_A = \frac{-Q}{4\pi\varepsilon_0 r} \qquad V_B = \frac{Q}{4\pi\varepsilon_0 r}$$

The resultant potential is:

$$V_A + V_B = \frac{-Q}{4\pi\varepsilon_0 r} + \frac{Q}{4\pi\varepsilon_0 r} = 0$$

at A and B are: The gravitational potentials due to the masses

$$V_A = \frac{-Gm}{r} \qquad V_B = \frac{-Gr}{r}$$

The resultant potential is:

$$V_A + V_B = \frac{-Gm}{r} - \frac{Gm}{r} = \frac{-2Gm}{r}$$

Review Exercise 13 (p.53)

A. Multiple Choice 到 Questions

surface. : $V_P = V_Q$. density is higher. And thus the electric field there is also And at deformed or sharp region, the surface charge A conductor has the same potential at any point on its

charge density at $Q < \sigma$.

electric intensity at Q < E.

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charges arrange themselves as far as possible from Because of the repulsion between like charges, the

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running through it is: charge is removed per second. And the area of belt

 $0.04 \times 0.8 = 0.032 \text{ m}^2 \text{ s}^{-1}$

Therefore, the charge density is:

harge density =
$$\frac{64 \times 10^{-6}}{\text{Area}}$$

= $\frac{64 \times 10^{-6}}{0.032}$
= $2.0 \times 10^{-3} \text{ C m}^{-2}$

α

$$\pi \varepsilon_0 r$$
 $4\pi \varepsilon_0 r$
It potential is:
 $-O$
 O

$$\frac{Gm}{r} \qquad V_B = \frac{-Gm}{r}$$

 $V_A + V_B = \frac{-Gm}{-} - \frac{Gm}{-} = \frac{-2Gm}{-}$

others. Therefore, charges appear only on the surface of The rate of charge leakage is 64 μ A. That means 64 μ C the sphere.

Charge density = Charge

By definition, potential gradient at a point is: Choice B (incorrect)

done required to move a unit positive charge from

By definition, electric potential at a point is the work

Choice A (incorrect)

infinity to that point.

$$\frac{dV}{dx} = -E$$

It is the negative of electric field at that point. Choice C (incorrect)

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electric field intensity at the sphere's surface just equal to surface. is determined by maximum electric field at the surface. And only choice D is a factor affecting electric field at air breakdown field. Therefore, the maximum potential The maximum potential is the potential at which the

$$E_{\text{max}} = \frac{Q}{4\pi\varepsilon_0 R^2}$$

R is the radius of the sphere.

the maximum potential. maximum potential. Other choices have no relation with Choice C is a factor affecting the time needed to reach

6.

equal. same. Therefore, the potentials of the two spheres are The potential at any point of a conductor is always the

spheres only transfer and arrange themselves to make the two spheres having the same potential. No charge is And by the conservation of charge, charges on the two Therefore, the charge is conserved being destroyed or created as the system is closed.

resistance. resistance, there is a loss of electrical energy against through the conducting wire. As wire prossesses And because there is a transfer of charges, current passes

Structured Questions

The relation between charge and electric potential is:

$$V = \frac{Q}{4\pi\varepsilon_0 R}$$

(a) For the sphere of 1.0 m radius,

Chapter 13 Electric Fields

$$1.0 \times 10^{6} = \frac{Q}{4\pi (8.85 \times 10^{-12})1}$$
$$Q = 1.11 \times 10^{-4} \text{ C}$$

(b) For the sphere of 1.0 cm radius,

$$1.0 \times 10^{6} = \frac{Q}{4\pi (8.85 \times 10^{-12})0.01}$$
$$Q = 1.11 \times 10^{-6} \text{ C}$$

(a) The total charge on the earth's surface is: Charge = Surface charge density \times Surface area = $(2.0 \times 10^{-19}) \times 4\pi (6.4 \times 10^{6})^{2}$

$$= (2.0 \times 10^{-1}) \times 4\pi (6.4 \times 10^{-1})^{-1}$$

$$= 1.03 \times 10^{-4} \text{ C}$$
The electric potential of earth is:
$$V = \frac{Q}{4\pi\varepsilon_0 R}$$

$$= \frac{1.03 \times 10^{-4}}{4\pi\varepsilon_0 (6.4 \times 10^6)}$$

(b) The electric field strength at a point close to the earth's surface is: = 0.145 V

$$E = \frac{Q}{4\pi\varepsilon_0 R^2} = \frac{V}{R}$$
$$= \frac{0.145}{6.4 \times 10^6} = 2.26 \times 10^{-8} \text{ V m}^{-1}$$

(a) Electric potential at point A is:

$$V_A = rac{Q}{4\piarepsilon_0} \cdot rac{1}{r_{QA}} = rac{Q}{4\piarepsilon_0} \cdot rac{1}{4} = rac{Q}{16\piarepsilon_0}$$

Electric potential at point *B* is:

$$V_B = \frac{\mathcal{Q}}{4\pi\varepsilon_0} \cdot \frac{1}{r_{\mathcal{Q}B}} = \frac{\mathcal{Q}}{4\pi\varepsilon_0} \cdot \frac{1}{3}$$

$$= \frac{\mathcal{Q}}{12\pi\varepsilon_0}$$
a notential difference between the

The potential difference between two points is:

$$|V_A - V_B| = \frac{Q}{\pi \varepsilon_0} \left| \left(\frac{1}{16} - \frac{1}{12} \right) \right|$$
$$= \frac{1.0 \times 10^{-6}}{\pi (8.85 \times 10^{-12})} (0.0208)$$
$$= 7.49 \times 10^2 \text{ V}$$

work is done by the charge. When a positive charge moves from B to A,

The work done is: W = Vq

= 0.1498 J $= (7.49 \times 10^2) \times (2.0 \times 10^{-4})$

10. (a) Coulomb's Law in electrostatics states that the electric field due to a charge Q is:

$$E = \frac{Q}{4\pi\varepsilon_0} \cdot \frac{1}{r^2} \propto \frac{1}{r^2}$$

proportional to the square of distance from the The magnitude of the electric field is inversely

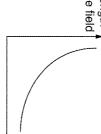
Similarly, Newton's Law of Gravitation states that the gravitational field due to a mass M is:

$$g = \frac{GM}{r^2} \propto \frac{1}{r^2}$$

The magnitude of gravitational field is also from the point. inversely proportional to the square of distance

below. The relation between strength and distance is shown proportional to the square of distance. These two are examples of the inverse square law field. The strength of this kind of field is inversely

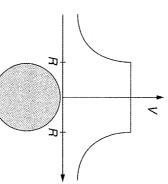
of the field Strength



- (b) Electric potential at a point is the energy required to Distance
- Moreover, electric potential is measured in Joules per Coulomb or in Volt, but electric potential and the external electric field. whether a charged object has been placed in that point. It is a property of electric field regardless of energy of a system consisting of the charged object field. However, electric potential energy is the bring a unit positive charge from infinity to that
- <u>c</u> Ξ energy is measured in Joules. negatively-charged rod is placed nearby, the electrons of the conductor repel and move to contain 'free electrons'. When a is always at the earth's potential. Conductors conductor carries a net positive charge. the earth through the wire. As a result, the When a conductor is connected to the earth, it

 Ξ conductor

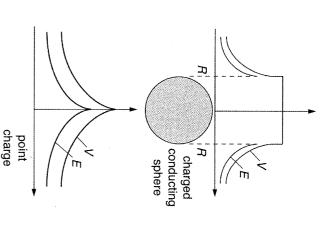
shown below: electric potential is generated as the graph Around the positively-charged sphere, positive



So, at the position of the conductor, the potential is positive.

And the conductor is isolated, although separated, it is always neutral (no net charge). positive charges and negative charges are

- 11. (a) (i) $\frac{\varepsilon}{4\pi\varepsilon_0 r^2}$ (ε_0 is the permittivity of free space)
- (ii) Only for points outside the conducting sphere. decrease with distance when r < R. sphere. This case is different from the case of symmetry and potential is a constant within the point charge, whose electric field and potential Inside a sphere, the electric field is zero by



(b) (i) energy of the He nucleus. Both He nucleus and Au nucleus are positively system (He & Au) is equal to the kinetic the He nucleus can reach should be the point where the electric potential energy of the Therefore, energy is needed to move the He By conservation of energy, the closest point nucleus towards the Au nucleus. charged, the force between them is repulsive.

$$\frac{1}{2}m_{\rm He}v^2 = \frac{Q_{\rm He}Q_{\rm Au}}{4\pi\varepsilon_0x}$$

The kinetic energy is: Q_{Au} -charge of Au, 79 positive charge $(Q_{
m He} ext{-}{
m charge}$ of He, 2 positive charge, M_{He} -mass of He, 2 neutrons and 2 protons)

 $\frac{1}{2}m_{\rm He}v^2$

 $= 1.64 \times 10^{-13} \text{ J}$ $\frac{1}{2}(2 \times 1.673 \times 10^{-27} + 2 \times 1.675 \times 10^{-27}) \times (7.0 \times 10^{6})^{2}$

And electric potential energy = kinetic ener;

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$$\frac{Q_{\text{He}}Q_{\text{Au}}}{4\pi\varepsilon_0 x} = 1.64 \times 10^{-13}$$

$$6.16 \times 10^{-19} \text{ }^2$$

 $2 \times 79 \times (1.6 \times 10^{-19})^2 = 1.64 \times 10^{-13}$ $4\pi(8.85\times10^{-12})x$

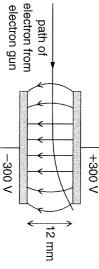
The gravitational attraction is negligible since (∵ The masses of He and Au are small.) than gravitational force the magnitude of electric force is much greater $x = 2.2 \times 10^{-13} \text{ m}$

> $\dot{\mathbf{U}}$ Overseas & HKALE Questions

> > Chapter 13

Electric Fields

(a) Drawn on Fig. (a), the direction of the electric field is from the positive plate to the negative plate.



(b) (i) Electric field strength Fig. (a)

$$E = \frac{1}{d}$$

$$= \frac{300 - (-300)}{12 \times 10^{-3}}$$

$$= 5.0 \times 10^{4} \text{ N C}^{-1}$$

- (ii) Force on an electron $= 8.0 \times 10^{-15} \,\mathrm{N}$ $= eE = (1.60 \times 10^{-19})(5.0 \times 10^4)$
- (c) Referring to Fig. (a), the electron will be deflected path. towards the positive plate, describing a parabolic
- 13. (a) (i) The gravitational force is a force of attraction inversely proportional to the square of their proportional to the product of the masses and is between masses with a magnitude that is
- Ξ Whereas the gravitational field strength at a point. force per unit mass acting on any object at that The electric potential V at a point in an electric point in a gravitational field is the gravitational
- a unit positive charge from infinity to the field E is defined as the work done in bringing

infinity to the point, i.e. U = qVwork done in bringing the charge q from charge q in an electric field is defined as the Whereas the electric potential energy U of a

- (b) (i) Charge on the gold nucleus
- = $n_{\rm p} \times e = 79 \times 1.60 \times 10^{-19} \,{\rm C}$ = $1.264 \times 10^{-17} = 1.26 \times 10^{-17} \,{\rm C}$

$$V = \frac{Q}{4\pi\varepsilon_0 r}$$

$$= \frac{1.264 \times 10^{-17}}{4\pi (8.85 \times 10^{-12})(2.5 \times 10^{-12})}$$

$$= 4.546 \times 10^4 = 45 \text{ kV}$$

 α -particle, ${}_{2}^{4}$ He, has 2 protons.

 $U = QV = (2 \times 1.60 \times 10^{-19})(4.546 \times 10^4)$ Electric potential energy of the α -particle $= 1.5 \times 10^{-14} \text{ J}$

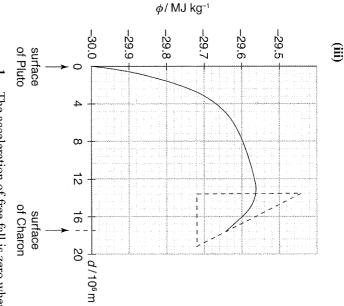
- ල (E) Relationship between the energies: $E_T = E_G + E_E$
- (ii) 1. In an α -particle scattering experiment, the electrical forces is in the order of 10^{-13} . ratio of the gravitational forces to the ignored in the experiment. Therefore gravitational effects are
- 2. The electric potential of the α -particle at a approach need not be considered. that position. Therefore the direction of independent of the path taken to reach distance r from the nucleus is
- 14. (a) (i) 1. The electric field strength at a point in an acting per unit positive charge placed at electric field is the electrostatic force that point.
- The electric potential at a point in an path taken. infinity to the point, irrespective of the charge in bringing the charge from electric field is the work done per unit

 $E = \frac{\Delta V}{}$ χ

 Ξ

Hence, the electric field strength at a point may versus distance from the point. at the point on the graph of electric potential be computed from the gradient of the tangent

- (b) All values of gravitational potential are two masses is always attractive. another, i.e. the gravitational force between negative because masses always attract one
- The gradient at a point on the graph of Fig. (a) equals the change in gravitational potential per is also the acceleration of free fall at that point. the point, according to the answer to (a)(ii) and magnitude of the gravitational field strength at unit distance from the surface. This equals the



- -The acceleration of free fall is zero where $= 13.6 \times 10^6 \text{ m}.$ acceleration of free fall is zero the surface of Pluto at which the zero. From the graph, the distance from the gradient of the graph in Fig. (a) is
- = gradient at d is equal to 15.4×10^6 m The acceleration of free fall on the surface of Charon $[-29.52 - (-29.76)] \times 10^{\circ}$ $(19.2-14.8)\times10^{6}$
- (c) (i) In order to reach Pluto, the rock must make it From that point to the surface of Pluto, fall is zero, i.e. where $d = 13.6 \times 10^6$ m. past the point where the acceleration of free = 0.055 m s⁻² (taking only the magnitude)

zero. velocity when its velocity at $d = 13.6 \times 10^6$ m is $\Delta \phi = [-29.565 - (-30)] \times 10^6 \,\mathrm{J \, kg}^{-1}$ change in potential, The rock reaches Pluto with the minimum $= 0.435 \times 10^6 \,\mathrm{J \, kg^{-1}}$

$$\therefore \frac{1}{2}mv^2 = m\Delta\phi$$

$$v = \sqrt{2\Delta\phi} = \sqrt{2 \times 0.435 \times 10^6}$$

$$= 933 \text{ m s}^{-1}$$

(ii) In order for the rock to travel from Pluto to between this point and the surface of Charon is $d = 13.6 \times 10^6$ m. The change in potential reaching Charon is less than that calculated smaller. Hence the minimum speed on Charon, it must make it past the point Ħ

15. – 16. HKALE Questions